# Who wants to be a millionaire <br> Computer Scientist? 

Preparation for the finals
Game 1

- If a breadth-first search starts at vertex $E$, the last vertex to be visited will be vertex $\qquad$ .


C D
D B

- If a breadth-first search starts at vertex E , the last vertex to be visited will be vertex $\qquad$ .


| C | 3 |
| :--- | :--- |
| D | 2 |

The correct answer is $\mathbf{C}$.

- At what position will we find 8 in the min-heap array below after we call dequeue()?

$$
\begin{array}{|l|l|l|l|l|l|l|l|}
\hline 2 & 3 & 6 & 8 & 10 & 15 & 18 & 25 \\
\hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7
\end{array}
$$

| $A$ | 0 |
| :--- | :--- |
| $B$ | 3 |


| C | 1 |
| :--- | :--- |
| D 5 |  |

- At what position will we find 8 in the min-heap array below after we call dequeue()?

$$
\begin{array}{|l|l|l|l|l|l|l|l|}
\hline 2 & 3 & 6 & 8 & 10 & 15 & 18 & 25 \\
\hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\
\hline
\end{array}
$$

| $A$ | 0 |
| :--- | :--- |
| $B$ | 3 |


| C | 1 |
| :--- | :--- |
| D | 5 |

The correct answer is C .

- Given the following table, where a hash function returns key $\% 11$, which values can be inserted sequentially without collision?
hashTable

| 0 | 11 |
| :---: | :---: |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| 6 |  |
| 7 |  |
| 8 |  |
| 9 |  |
| 10 |  |


| $A$ | $22,33,44$ |
| :--- | :--- |
| $B$ | $23,35,47$ |


| $C$ | $23,34,45$ |
| :--- | :--- |
| $D$ | $22,34,45$ |

- Given the following table, where a hash function returns key $\% 11$, which values can be inserted sequentially without collision?
hashTable

| 0 | 11 |
| :---: | :---: |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| 6 |  |
| 7 |  |
| 8 |  |
| 9 |  |
| 10 |  |


| $A$ | $22,33,44$ |
| :--- | :--- |
| $B$ | $23,35,47$ |


| $C$ | $23,34,45$ |
| :--- | :--- |
| $D$ | $22,34,45$ |

The correct answer is $B$.

- Assuming that a breadth-first search starts at $E$, which vertices are in the Queue after vertices E, G, and D have been processed?


| $A$ | $A, C$ |
| :--- | :--- |
| $B$ | $E, G$ |

$$
\begin{array}{ll}
\hline C & A, C, G \\
D & A, C, E, G \\
\hline
\end{array}
$$

- Assuming that a breadth-first search starts at $E$, which vertices are in the Queue after vertices E, G, and D have been processed?


| $A$ | $A, C$ |
| :--- | :--- |
| $B$ | $E, G$ |


| $C$ | $A, C, G$ |
| :--- | :--- |
| $D$ | $A, C, E, G$ |

The correct answer is A.

- Using double hashing, how do we determine the first index when inserting item 20?

$$
\begin{aligned}
& \text { hash1(key) }=\text { key } \% 11 \\
& \text { hash2(key) }=5-\text { key } \% 5
\end{aligned}
$$

and a hash table with a size of 10
A. $(20 \% 11+1$ * (5-20 \% 5)) $\% 10$
B. $(20 \% 11+0$ * $(5-20 \% 5)) \% 11$
C. $(20 \% 11+0$ * $(5-20 \% 5)) \% 10$
D. $\left(20 \% 11+1^{*}(5-20 \% 5)\right) \% 11$


| $C$ |
| :--- |
| $D$ |

- Using double hashing, how do we determine the first index when inserting item 20?

$$
\begin{aligned}
& \text { hash1(key) }=\text { key } \% 11 \\
& \text { hash2(key) }=5-\text { key } \% 5
\end{aligned}
$$

and a hash table with a size of 10
A. $(20 \% 11+1$ * (5-20 \% 5)) $\% 10$
B. $(20 \% 11+0$ * $(5-20 \% 5)) \% 11$
C. $(20 \% 11+0$ * $(5-20 \% 5)) \% 10$
D. $\left(20 \% 11+1^{*}(5-20 \% 5)\right) \% 11$

| $A$ |
| :--- |
| $B$ |


| C |
| :--- |
| D |

The correct answer is $C$.

Checkpoint 1 reached!
You have 5,000 points

- Identify the new priority queue after enqueueing 40 into the minheap array shown below.

| 29 | 36 | 42 | 54 |
| :--- | :--- | :--- | :--- |

A | 29 | 36 | 42 | 54 | 40 |
| :--- | :--- | :--- | :--- | :--- |

C | 29 | 36 | 40 | 42 | 54 |
| :--- | :--- | :--- | :--- | :--- |

B | 40 | 29 | 36 | 42 | 54 |
| :--- | :--- | :--- | :--- | :--- |

D | 29 | 36 | 42 | 40 | 54 |
| :--- | :--- | :--- | :--- | :--- |



C
D

- Identify the new priority queue after enqueueing 40 into the minheap array shown below.

| 29 | 36 | 42 | 54 |
| :--- | :--- | :--- | :--- |

A | 29 | 36 | 42 | 54 | 40 |
| :--- | :--- | :--- | :--- | :--- |

C | 29 | 36 | 40 | 42 | 54 |
| :--- | :--- | :--- | :--- | :--- |

B | 40 | 29 | 36 | 42 | 54 |
| :--- | :--- | :--- | :--- | :--- |

D | 29 | 36 | 42 | 40 | 54 |
| :--- | :--- | :--- | :--- | :--- |

| $A$ |
| :--- |
| $B$ |

C
The correct answer is C .

- What is the cost of the shortest path from $Y$ to $U$ in the following graph?



## C 12

D Something else

- What is the cost of the shortest path from $Y$ to $U$ in the following graph?


| $A$ | 11 |
| :--- | :--- |
| $B$ | $\infty$ |

C 12
D Something else
The correct answer is B.

- After resizing a hash table with 13 buckets, the new size will be
$\qquad$ .


| C | 23 |
| :--- | :--- |
| D | 31 |

- After resizing a hash table with 13 buckets, the new size will be
$\qquad$ .

| $A$ | 26 |
| :--- | :--- |
| $B$ | 29 |


| C | 23 |
| :--- | :--- |
| D | 31 |

The correct answer is B.

- Identify the minimum spanning tree for the following graph:



A


B


C


D

| $A$ |
| :--- |
| $B$ |



- Identify the minimum spanning tree for the following graph:



A


B


C


D

| C |
| :--- |
| D |

The correct answer is B.

- Identify the order in which the vertices are discovered during a (nonrecursive) DFS traversal of the graph starting with vertex B.


C $\quad$ B,D,C,E,A

- Identify the order in which the vertices are discovered during a (nonrecursive) DFS traversal of the graph starting with vertex B.


| C | $B, D, C, E, A$ |
| :--- | :--- |
| $D$ | $B, C, E, A, D$ |

The correct answer is D .

## Checkpoint 2 reached!

You have 50,000 points

## Question 11. 75,000 points

- Identify the new max-heap-array created after the heapify operation of the following array:

| 47 | 25 | 36 | 60 | 54 |
| :--- | :--- | :--- | :--- | :--- |


$A$| 25 | 36 | 47 | 54 | 60 |
| :--- | :--- | :--- | :--- | :--- |

C | 60 | 54 | 36 | 25 | 47 |
| :--- | :--- | :--- | :--- | :--- |

B | 25 | 47 | 36 | 60 | 54 |
| :--- | :--- | :--- | :--- | :--- |

D | 60 | 54 | 47 | 36 | 25 |
| :--- | :--- | :--- | :--- | :--- |



| C |
| :--- |
| D |

## Question 11. 75,000 points

- Identify the new max-heap-array created after the heapify operation of the following array:

| 47 | 25 | 36 | 60 | 54 |
| :--- | :--- | :--- | :--- | :--- |

A | 25 | 36 | 47 | 54 | 60 |
| :--- | :--- | :--- | :--- | :--- |

C | 60 | 54 | 36 | 25 | 47 |
| :--- | :--- | :--- | :--- | :--- |

B | 25 | 47 | 36 | 60 | 54 |
| :--- | :--- | :--- | :--- | :--- |

D | 60 | 54 | 47 | 36 | 25 |
| :--- | :--- | :--- | :--- | :--- |



| C |
| :--- |
| D |

The correct answer is C.

- Consider a hash table of size 100.
- Which hash function produces the fewest number of collisions for keys 10, 20, 30, 40, 50, and 60?

| A | key \% 6 |
| :--- | :--- |
| B | key \% 50 |


| C | key \% 10 |
| :--- | :--- |
| D | key \% 5 |

- Consider a hash table of size 100.
- Which hash function produces the fewest number of collisions for keys 10, 20, 30, 40, 50, and 60?

| A | key \% 6 |
| :--- | :--- |
| B | key \% 50 |


| C | key \% 10 |
| :--- | :--- |
| D | key \% 5 |

## Question 13. 250,000 points

- How many times do we call siftDown (percolateDown) while sorting the following array using heapsort?

| 47 | 54 | 60 | 25 | 36 | 13 | 90 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| $A$ | 6 |
| :--- | :--- |
| $B$ | 9 |


| C | 12 |
| :--- | :--- |
| D | 18 |

## Question 13. 250,000 points

- How many times do we call siftDown (percolateDown) while sorting the following array using heapsort?

| 47 | 54 | 60 | 25 | 36 | 13 | 90 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| $A$ |
| :--- |
| $B$ |



## The correct answer is B.

- What is the DGS of nodes C,D,E,F in the next iteration of the Dijkstra's algorithm?


| $A$ | $C: 6, D: 8, E: 5, F: 5$ |
| :--- | :--- |
| $B$ | $C: 8, D: 13, E: 7, F: 7$ |


| $C$ | $C: 8, D: 4, E: 7, F: 7$ |
| :--- | :--- |
| $D$ | $C: 6, D: 4, E: 5, F: 5$ |

- What is the DGS of nodes C,D,E,F in the next iteration of the Dijkstra's algorithm?


|  | Iteration 1 |  | Iteration 2 |  |
| :---: | :---: | :---: | :---: | :---: |
|  | X | $\mathrm{V}-\mathrm{X}$ | X | $\mathrm{V}-\mathrm{X}$ |
|  | cost | DGS | cost | DGS |
| A | 0 |  | 0 |  |
| B |  | 2 | 2 |  |
| C |  | $\infty$ |  | 8 |
| D |  | 4 |  | 4 |
| E |  | $\infty$ |  | 7 |
| F |  | $\infty$ |  | 7 |


| $A$ | $C: 6, D: 8, E: 5, F: 5$ |
| :--- | :--- |
| $B$ | $C: 8, D: 13, E: 7, F: 7$ |


| $C$ | $C: 8, D: 4, E: 7, F: 7$ |
| :--- | :--- |
| $D$ | $C: 6, D: 4, E: 5, F: 5$ |

- Identify the order in which the vertices are discovered and processed during a (recursive) DFS traversal of the following graph starting with vertex A.


| A | Discovery: ABCDE <br> Processing: EDCBA |
| :---: | :--- |
| B | Discovery: ABDCE <br> Processing: ECDBA |

C Discovery: ABCDE Processing: CBEDA
D Discovery: ABCDE Processing: ABCDE

- Identify the order in which the vertices are discovered and processed during a (recursive) DFS traversal of the following graph starting with vertex A.


| A | Discovery: ABCDE <br> Processing: EDCBA |
| :--- | :--- |
| B | Discovery: ABDCE <br> Processing: ECDBA |


| C | Discovery: ABCDE <br> Processing: CBEDA |
| :--- | :--- |
| D | Discovery: ABCDE Processing: <br> ABCDE |

The correct answer is $\mathbf{C}$.

## Well done!

You are almost ready for the final exam

