# MINING FLIPPING CORRELATIONS FROM LARGE DATASETS WITH TAXONOMIES 

MARINA BARSKY, SANGKYUM KIM,<br>TIM WENINGER, JIAWEI HAN

## Outline

$\square$ Challenge: strong correlations with low support
$\square$ Flipping correlation patterns
$\square$ Algorithm for mining flipping correlations
$\square$ Performance
$\square$ Real flipping patterns
$\square$ Conclusion and future work

## Correlations and frequent itemsets

$\square$ Once all frequent itemsets are enumerated, we can find correlation between items in these frequent itemsets
$\square$ Computation of frequent itemsets is feasible only for high support thresholds
$\square$ Top-frequent itemsets often represent obvious relationships between items

## Example: frequent items in papers on frequent pattern mining



## Challenge of finding itemsets with low

 supportIn large datasets we can find the top most frequent itemsets
$\square$ When we lower the support threshold, the number of frequent itemsets becomes big
$\square$ How big? Very big: that we cannot keep in memory all different 2 -item combinations, to update their counters

## How can we discover non-trivial correlations in large datasets?

$\square$ Instead of computing top-frequent, compute topcorrelated patterns directly, without enumerating all frequent itemsets
$\square$ This presents computational challenges
$\square$ Some progress in this direction is in our previous paper

## Negative correlations

$\square$ What if we are also interested in items that rarely appear in the same transaction?
$\square$ The negative correlations can be useful:
$\square$ To identify competing items: absence of Blu ray and DVD player in the same transaction
$\square$ To discover underrepresented topic combinations: in DBLP -\{mobile networks, data cube\}
$\square$ The set of all itemsets where items are negatively correlated is exponentially large and "the solution remains elusive"
P.-N. Tan et al., 2005.

Challenge: all positive and negative correlations in itemsets with low-to-medium support
$\square$ Computing all frequent itemsets with very low support is computationally prohibitive
$\square$ Most of the correlation measures for large datasets possess neither monotonicity nor anti-monotonicity properties, and as such cannot be straightforwardly used for pruning purposes.

## Outline

- Challenge: strong correlations with low support
$\square$ Flipping correlation patterns
$\square$ Algorithm for mining flipping correlations
$\square$ Performance
$\square$ Real flipping patterns
$\square$ Conclusion and future work


## Feasible task with the use of taxonomy

$\square$ We cannot compute all positive and negative correlations with low support
$\square$ We can find the most surprising positive and negative correlations, which change across the levels of abstraction
$\square$ Items at different levels of abstraction can be modeled as a taxonomy tree

## Example of taxonomy: movies



## Example: flipping correlations in Movielens dataset



People who like westerns do not like romance movies (negative correlation)

Despite this general rule, people who like High Noon (western) also like The big Country (romance) (positive correlation)

Flipping Correlation Example

## Flipping correlations are surprising

$\square$ If two groups of items are negatively correlated, but some sub-groups are positively correlated. What is so special about them?
$\square$ The positive correlation between two groups of items suggest that the items in both groups behave similarly. But some sub-groups are negatively correlated. Why?
$\square$ We leave these questions to domain experts, and our contribution is an efficient computation of all flipping correlations

## Outline

- Challenge: strong correlations with low support
- Flipping correlation patterns
$\square$ Algorithm for mining flipping correlations
$\square$ Performance
$\square$ Real flipping patterns
$\square$ Conclusion and future work


## Selecting correlation measure

## Two groups of correlation measures

$\square$ Null-invariant
$\square$ Expectation-based

Null-(transaction)
invariance is crucial for large datasets

| Measure | Definition | Range | Null-Invariant |
| :---: | :---: | :---: | :---: |
| $\chi^{2}(a, b)$ | $\sum_{i, j=0,1} \frac{\left(e\left(a_{i}, b_{j}\right)-o\left(a_{i}, b_{j}\right)\right)^{2}}{e\left(a_{i}, b_{j}\right)}$ | $[0, \infty]$ | No |
| Lift (a, b) | $\frac{P(a b)}{P(a) P(b)}$ | $[0, \infty]$ | No |
| AllConf ( $a, b$ ) | $\frac{\sup (a b)}{\max \{\sup (a), \sup (b)\}}$ | [0,1] | Yes |
| Coherence ( $a, b$ ) | $\frac{\sup (a b)}{\sup (a)+\sup (b)-s u p(a b)}$ | [0,1] | Yes |
| Cosine ( $a, b$ ) | $\frac{\sup (a b)}{\sqrt{\sup (a) \sup (b)}}$ | $[0,1]$ | Yes |
| Kulc (a,b) | $\frac{\sup (a b)}{2}\left(\frac{1}{\sup (a)}+\frac{1}{\sup (b)}\right)$ | [0, 1] | Yes |
| MaxConf (a,b) | $\max \left\{\frac{\sup (a b)}{\sup (a)}, \frac{\sup (a b)}{\sup (b)}\right\}$ | $[0,1]$ | Yes |

T. Wu et al., 2010.

## Challenge with null-invariant measures

$\square$ Some (Cosine, Kulczynsky) are not anti-monotone
$\square$ We cannot extract flipping correlations by postprocessing all positive and negative correlations, since we cannot compute all positive and negative correlations (see slide 8)
$\square$ Solution: incorporate flipping constraints into a mining process

## Flipper algorithm:

## based on three main pruning techniques

1. Pruning non-flipping itemsets
2. Termination of the entire pattern growth
3. Pruning single items and their supersets

## 1. Pruning non-flipping patterns (I)

$\square$ If both parent itemset ( $a b$ ) and child itemset $\left(a_{1} b_{2}\right)$ have the same correlation sign, then they break a flipping sequence and the children of $a_{1} b_{2}$ cannot be a part of flipping pattern - do not test them


## 1. Pruning non-flipping patterns (II)

$\square$ However, $a$ superset of child itemset $\left(a_{12} b_{12}\right)$ can still be a part of a flipping pattern, since we cannot predict the correlation value of its superset (not antimonotone).


Vertical pruning if it is not flipping

## 2. Termination of the Entire Pattern Growth

$\square$ We prove that for any null-invariant correlation measure, correlation of the superset cannot be larger than the max of correlations of its subsets

$$
\operatorname{Corr}\left(a_{1}, \cdots, a_{n+1}\right) \leq \max \left(\operatorname{Corr}\left(a_{1}, \cdots, a_{n}\right), \cdots, \operatorname{Corr}\left(a_{2}, \cdots, a_{n+1}\right)\right)
$$

## 2. Termination of the Entire Pattern

 Growth$$
\operatorname{Corr}\left(a_{1}, \cdots, a_{n+1}\right) \leq \max \left(\operatorname{Corr}\left(a_{1}, \cdots, a_{n}\right), \cdots, \operatorname{Corr}\left(a_{2}, \cdots, a_{n+1}\right)\right)
$$

If we adding items to itemsets, and we found that all itemsets in two consecutive cells are non-positive, then there are no more flipping patterns because supersets cannot be positively correlated

We can stop our search right there

|  |  | k-itemsets |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathrm{k}=2$ | k=3 | ... | k=K |
|  | $\mathrm{h}=1$ |  | $\square$ |  |  |
|  | $\mathrm{h}=2$ |  | ص |  |  |
|  | ! |  |  |  |  |
|  | $h=\mathrm{H}-1$ |  |  |  |  |

## 3. Pruning single items and their supersets

$\square$ If all itemsets containing item $a_{1}$ are non-positive, and all itemsets containing its generalization item a are non-positive, then item $a_{1}$ and all its supersets can be removed from further consideration


## Order of computation

$\square$ To utilize these pruning principles, we need to always compare results for two vertically consecutive cells


These are the main ideas of the Flipper algorithm

## Outline

$\checkmark$ Challenge: strong correlations with low support
Flipping correlation pattern
$\checkmark$ Algorithm for mining flipping correlations
$\square$ Performance
$\square$ Real flipping patterns
$\square$ Conclusion and future work

## Performance: Synthetic datasets

$\square$ Running Time (sec)




Flipper scales gracefully with the increase of the number of transactions and the average number of items per transaction

## Performance: real datasets

$\square$ Data Sets

|  | \# Trans | \# Pos | \# Neg | \# Flips |
| :---: | :---: | :---: | :---: | :---: |
| GROCERIES | 10 K | 4.8 K | 80 K | 174 |
| CENSUS | 32 K | 140 K | 73 K | 232 |
| MEDLINE | 6.4 M | 4.2 K | 1.6 M | 430 |

$\square$ Running Time (sec)
$\square$ Basic is not included (ran more than 10 hours for the smallest dataset GROCERIES).


## Outline

V Challenge: strong correlations with low support
Flipping correlation pattern
V Algorithm for mining flipping correlations
$\checkmark$ Performance
$\square$ Real flipping patterns
$\square$ Conclusion and future work

## Flipping patterns: discover incorrectly classified items



GROCERIES

Re-design store layouts
$\square$ pork and salad dressing are positively correlated, while in general meat and delicatessen are negatively correlated.
$\square$ This might suggest removing the salad dressing from delicatessen, and moving it closer to the meat department.

## Flipping patterns: contrasting sub-populations



CENSUS

Discover sub-populations with a distinct behaviour
$\square$ People working in Craftrepair and having Bachelor degree are positively correlated with high income, unlike all people working in
Craft-repair
$\square$ Education matters

## Flipping patterns:

## under-represented item combinations



Suggest under-represented research topic combinations
$\square$ This pattern suggests the collaboration between two unrelated areas of psychophysiology and psychotherapy.
$\square$ However, if one decides to study the combination of such subtopics as biofeedback and behavior therapy, he finds out that these two are in fact often studied together.

## Flipping patterns in real datasets



GROCERIES


CENSUS


MEDLINE

## Outline

V Challenge: strong correlations with low support
Flipping correlation pattern
V Algorithm for mining flipping correlations
$\checkmark$ Performance
V Real flipping patterns
$\square$ Conclusion and future work

## Summary

$\square$ Introduced the notion of a flipping correlation pattern.
$\square$ Developed the Flipper algorithm for mining these patterns.
$\square$ Algorithm is based on flipping constraints and mathematical properties shared among all null-invariant correlation measures
$\square$ Demonstrated the high efficiency of Flipper in experiments with low support thresholds
$\square$ Have shown that interesting new patterns can be extracted using the flipping pattern concept.

## Future work

$\square$ More advanced data structures for improving performance of Flipper
$\square$ Top-K "most flipping" patterns
$\square$ Computing a set of all discriminative correlations specific for a given subgroup

# Thank you for listening 

Please email your questions and suggestions to: mgbarsky@gmail.com

