

# Relational-algebra exercises on Pizza dataset

Solutions

# Setup

Person ( name, age, gender )

Frequents ( name, pizzeria )

Eats ( name, pizza )

Serves ( pizzeria, pizza, price )

- Eats contains information about what type of pizza each person (customer) eats (likes)
- Name is always the customer's name
- Frequents record information about pizzerias that each customer frequents (visits)
- Serves contains information about all possible pizza types for each pizzeria

Person ( name, age, gender )

Frequents ( name, pizzeria )

Eats ( name, pizza )

Serves ( pizzeria, pizza, price )

9. Find the names of all females who eat either mushroom or pepperoni pizza (or both).

$\pi_{\text{name}}(\sigma_{\text{gender}='female' \text{ AND } (\text{pizza}='mushroom' \text{ OR } \text{pizza}='pepperoni')}(Person \bowtie Eats))$

Person ( name, age, gender )

Frequents ( name, pizzeria )

Eats ( name, pizza )

Serves ( pizzeria, pizza, price )

10. Find the names of all females who eat both mushroom and pepperoni pizza.

$$\pi_{\text{name}} \left( \sigma_{\text{gender}='female' \text{ AND } \text{pizza}='mushroom'} (\text{Person} \bowtie \text{Eats}) \right) \cap$$
$$\pi_{\text{name}} \left( \sigma_{\text{gender}='female' \text{ AND } \text{pizza}='pepperoni'} (\text{Person} \bowtie \text{Eats}) \right)$$

Person ( name, age, gender )

Frequents ( name, pizzeria )

Eats ( name, pizza )

Serves ( pizzeria, pizza, price )

11. Find all pizzerias that serve at least one pizza that Amy eats for less than \$10.00.

$\pi_{\text{pizzeria}}(\sigma_{\text{name}='Amy'}(\text{Eats}) \bowtie \sigma_{\text{price} < 10}(\text{Serves}))$

Person ( name, age, gender )

Frequents ( name, pizzeria )

Eats ( name, pizza )

Serves ( pizzeria, pizza, price )

12. Find all pizzerias frequented by at least one person under the age of 18.

$$\pi_{\text{pizzeria}}(\sigma_{\text{age} < 18}(\text{Person}) \bowtie \text{Frequents})$$

Person ( name, age, gender )

Frequents ( name, pizzeria )

Eats ( name, pizza )

Serves ( pizzeria, pizza, price )

13. Find all pizza types which are not eaten by anyone

$\pi_{\text{pizza}}(\text{Serves}) - \pi_{\text{pizza}}(\text{Eats})$

Person ( name, age, gender )

Frequents ( name, pizzeria )

Eats ( name, pizza )

Serves ( pizzeria, pizza, price )

14. Find all pizzerias that are frequented by only females or only males.

$$\left[ \begin{array}{l} \pi_{\text{pizzeria}}(\sigma_{\text{gender}='female'}(\text{Person}) \bowtie \text{Frequents}) - \\ \pi_{\text{pizzeria}}(\sigma_{\text{gender}='male'}(\text{Person}) \bowtie \text{Frequents}) \end{array} \right] \cup$$

$$\left[ \begin{array}{l} \pi_{\text{pizzeria}}(\sigma_{\text{gender}='male'}(\text{Person}) \bowtie \text{Frequents}) - \\ \pi_{\text{pizzeria}}(\sigma_{\text{gender}='female'}(\text{Person}) \bowtie \text{Frequents}) \end{array} \right]$$



Person ( name, age, gender )

Frequents ( name, pizzeria )

Eats ( name, pizza )

Serves ( pizzeria, pizza, price )

15. Find all pizzerias where Dan could buy pizzas that he eats, and where he has never bought a pizza yet

$\pi_{\text{pizzeria}} [ (\sigma_{\text{name}='Dan'}(\text{Eats})) \bowtie (\text{Serves}) ]$

-

$\pi_{\text{pizzeria}} (\sigma_{\text{name}='Dan'}(\text{Frequents}))$

Person ( name, age, gender )

Frequents ( name, pizzeria )

Eats ( name, pizza )

Serves ( pizzeria, pizza, price )

16. For each person, find all pizzas the person eats that are not served by any pizzeria the person frequents. Return all such person (name, pizza) pairs.

$Eats - \pi_{\text{name, pizza}}(\text{Frequents} \bowtie \text{Serves})$

Person ( name, age, gender )

Frequents ( name, pizzeria )

Eats ( name, pizza )

Serves ( pizzeria, pizza, price )


17. Find the names of all people who frequent only pizzerias serving at least one pizza they eat.

$\pi_{\text{name}}(\text{Person})$

–

$\pi_{\text{name}}(\text{Frequents} - \pi_{\text{name,pizzeria}}(\text{Eats} \bowtie \text{Serves}))$

Explanation  
on the next  
page



17. Find the names of all people who frequent only pizzerias serving at least one pizza they eat.

- 1. List of all pizzerias which serve at least one of pizzas which particular person can eat:

$\pi_{\text{name,pizzeria}}(\text{Eats} \bowtie \text{Serves})$

- 2. List of all pizzerias which are frequented by this person but do not serve any pizza he can it

Frequents -  $\pi_{\text{name,pizzeria}}(\text{Eats} \bowtie \text{Serves})$

- 3. Answer to the query

$\pi_{\text{name}}(\text{Person})$

-

$\pi_{\text{name}}(\text{Frequents} - \pi_{\text{name,pizzeria}}(\text{Eats} \bowtie \text{Serves}))$

Person ( name, age, gender )

Frequents ( name, pizzeria )

Eats ( name, pizza )

Serves ( pizzeria, pizza, price )


18. Find the names of all people who frequent every pizzeria serving at least one pizza they eat.

$\pi_{\text{name}}(\text{Person})$

–

$\pi_{\text{name}}(\pi_{\text{name,pizzeria}}(\text{Eats} \bowtie \text{Serves}) - \text{Frequents})$

Explanation  
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18. Find the names of all people who frequent every pizzeria serving at least one pizza they eat.

➤ 1. List of all pizzerias per person which serve at least one pizza this person can eat:

$\pi_{\text{name,pizzeria}}(\text{Eats} \bowtie \text{Serves})$

➤ 2. List of pizzerias which serve the desirable pizza but which person did not visit yet

$\pi_{\text{name,pizzeria}}(\text{Eats} \bowtie \text{Serves}) - \text{Frequents}$

➤ 3. All the people excluding those in p.2

$\pi_{\text{name}}(\text{Person})$

–

$\pi_{\text{name}}(\pi_{\text{name,pizzeria}}(\text{Eats} \bowtie \text{Serves}) - \text{Frequents})$

Person ( name, age, gender )  
 Frequents ( name, pizzeria )  
 Eats ( name, pizza )  
 Serves ( pizzeria, pizza, price )

19. Find the pizzeria serving the cheapest pepperoni pizza. In the case of ties, return all of the cheapest-pepperoni pizzerias.

$\pi_{\text{pizzeria}}(\sigma_{\text{pizza}='pepperoni'}\text{Serves})$


–

$\pi_{\text{pizzeria}} [ \sigma_{\text{price} > \text{price2}} ( \pi_{\text{pizzeria}, \text{price}} (\sigma_{\text{pizza}='pepperoni'}\text{Serves})$

×

$\rho_{\text{pizzeria2}, \text{price2}} \pi_{\text{pizzeria}, \text{price}} (\sigma_{\text{pizza}='pepperoni'}\text{Serves})) ] ]$

Explanation  
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19. Find the pizzeria serving the cheapest pepperoni pizza. In the case of ties, return all of the cheapest-pepperoni pizzerias.

- 1. Finds all pizzerias where price for pepperoni pizza is greater than in some other pizzeria

$$\sigma_{\text{price} > \text{price2}} \left( \pi_{\text{pizzeria,price}} (\sigma_{\text{pizza}='pepperoni'} \text{Serves}) \right) \times \rho_{\text{pizzeria2,price2}} \left[ \pi_{\text{pizzeria,price}} (\sigma_{\text{pizza}='pepperoni'} \text{Serves}) \right]$$

- 2. Subtracts it from all other pizzerias serving pepperoni pizzas

$$\pi_{\text{pizzeria}} (\sigma_{\text{pizza}='pepperoni'} \text{Serves}) - \pi_{\text{pizzeria}} \left[ \sigma_{\text{price} > \text{price2}} \left( \pi_{\text{pizzeria,price}} (\sigma_{\text{pizza}='pepperoni'} \text{Serves}) \right) \times \rho_{\text{pizzeria2,price2}} \left( \pi_{\text{pizzeria,price}} (\sigma_{\text{pizza}='pepperoni'} \text{Serves}) \right) \right]$$